

# Multistage Stochastic Optimal Operation of Energy-Efficiency Building with CHP System

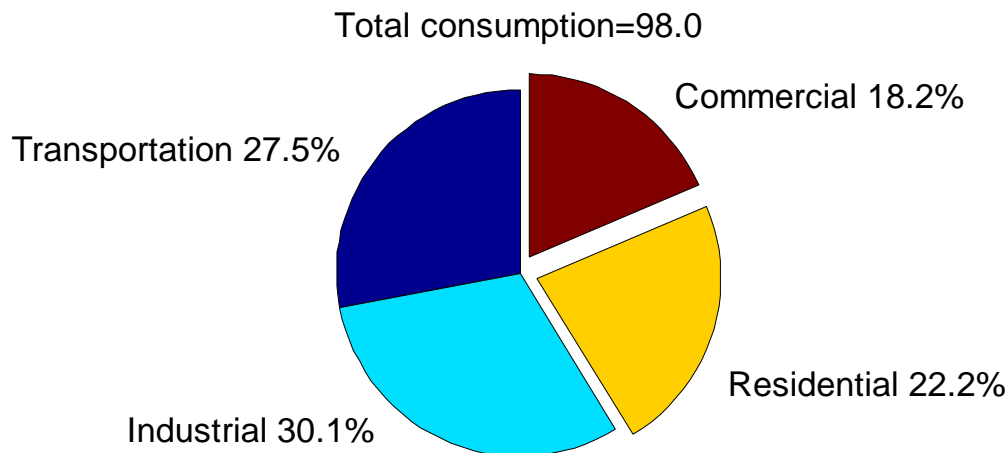
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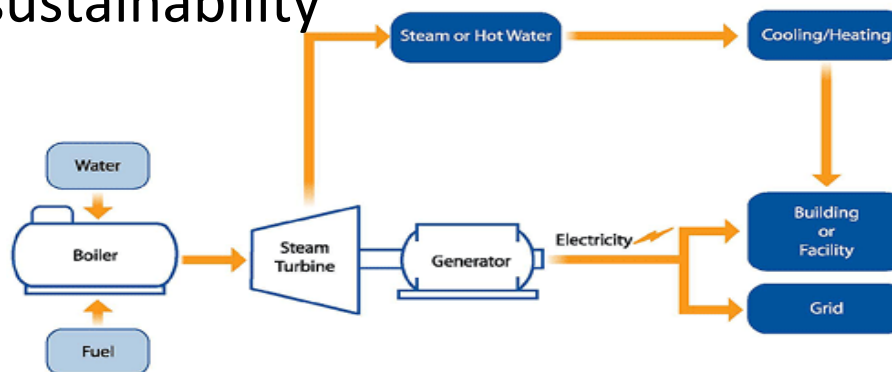
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# Introduction

- The operation of energy buildings have a surprisingly profound influence on the natural environment, health, economy, and productivity

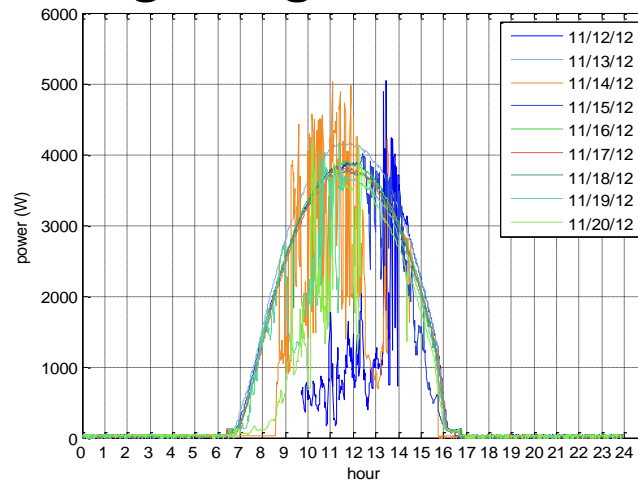


- Combined heat and power (CHP) systems are essential to efficiently reduce global energy use in buildings and improve the local environmental sustainability



# Motivations

- Due to the global warming mitigation and depletion of energy resources, renewable energy like small wind farms and photovoltaic plants are getting interest in distribution systems.



- Load forecasting technique is essential to achieve efficient load management. Actual demand of individual households varies over time depending on the outside temperature seasons and end-user behavior.



Distribution system



CHP with Boiler



Battery



Building system



Refrigerator



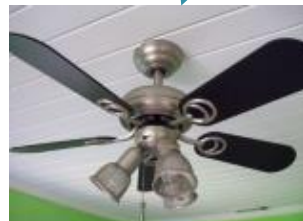
Microwave Oven



Air Conditioner



Washing Machine



Ceiling Fan

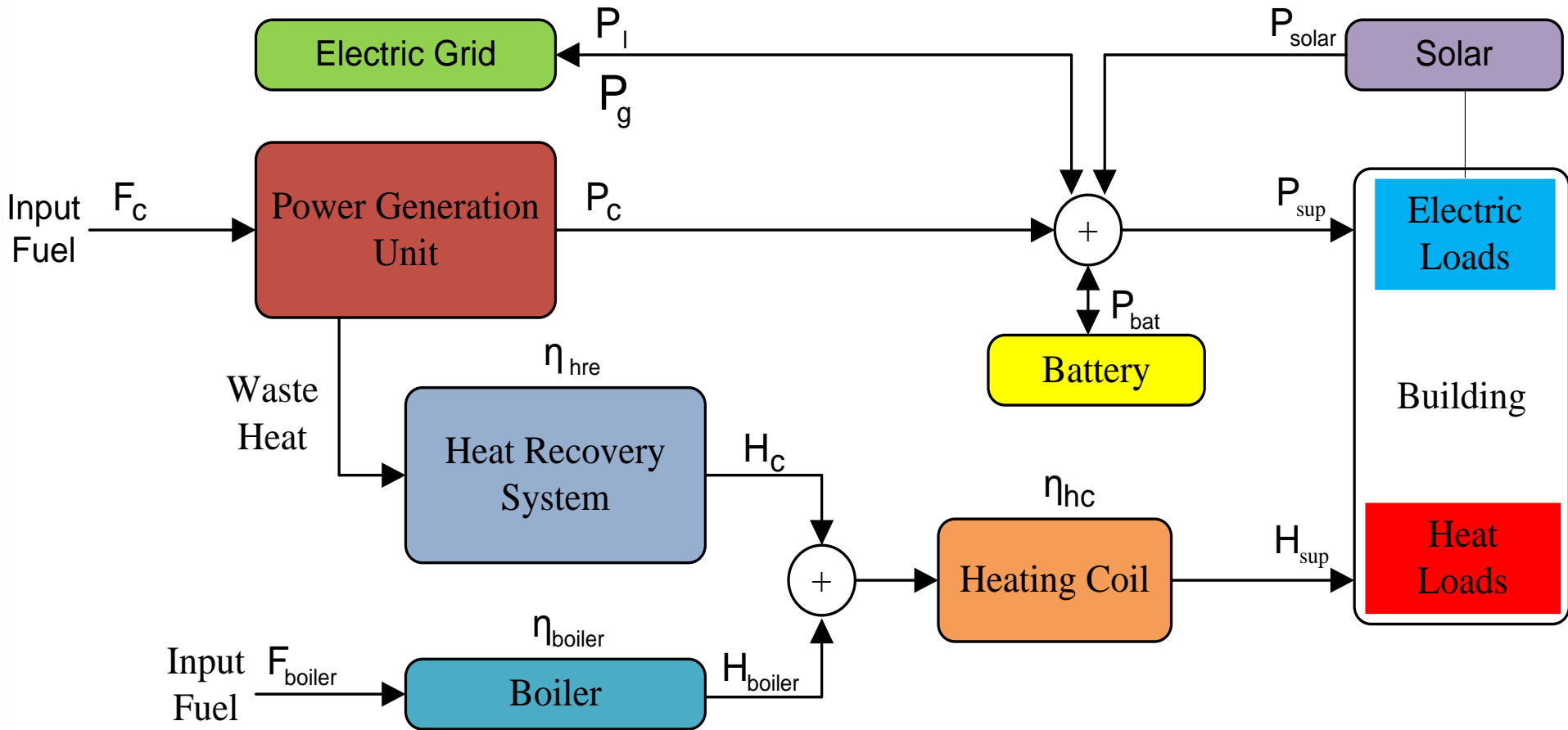


PC



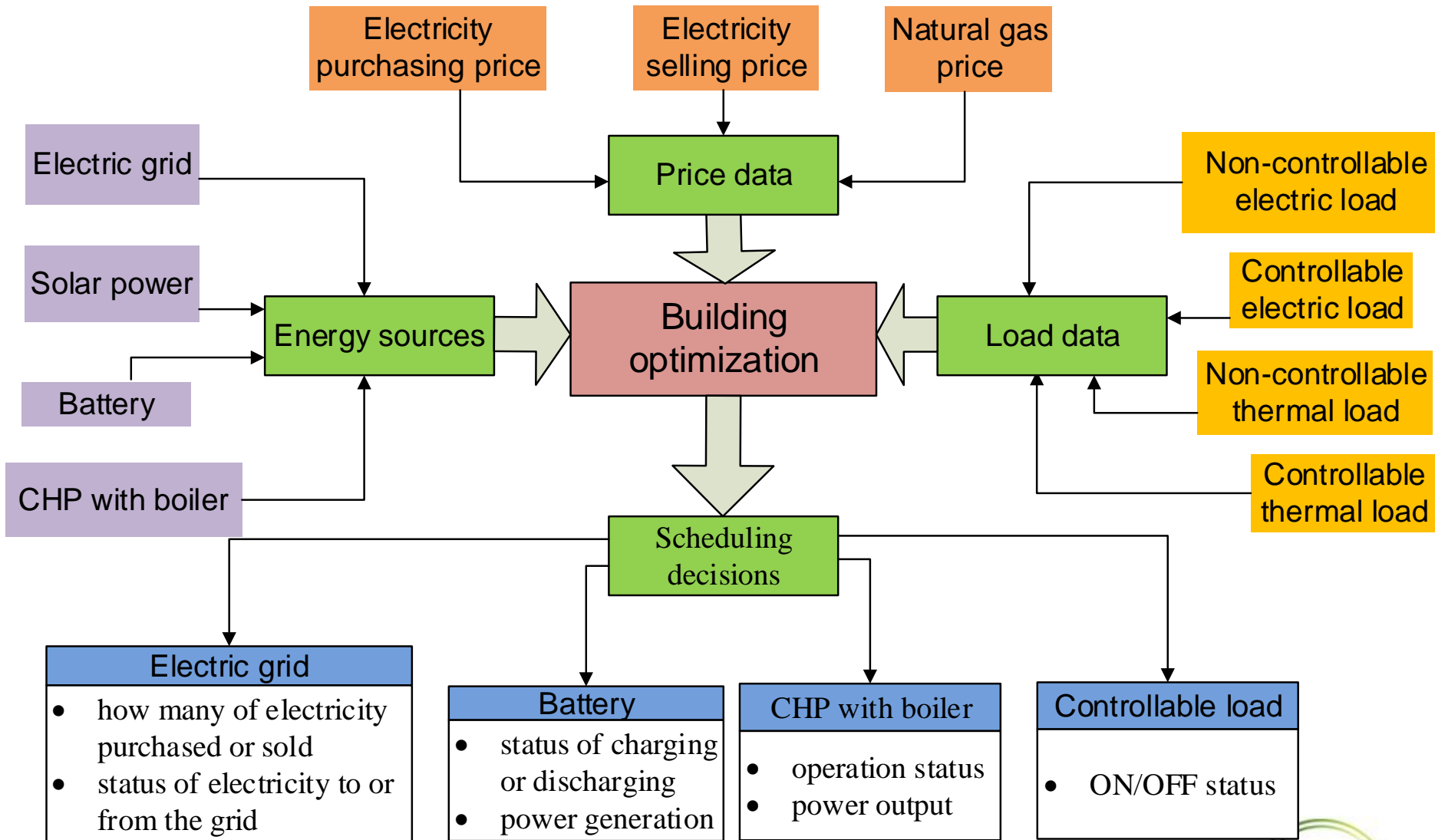
TV

# System Modeling



Energy flow diagram of energy-efficiency building

# Problem Description



# Stochastic Programming Model

$$\begin{aligned} \text{Min} \quad & C_{gf,1} \cdot P_{gf,1} - C_{gt,1} \cdot P_{gt,1} + C_{gas,1} \cdot (F_{chp,1} + F_{boi,1}) \\ & + \sum_{t=2}^T \sum_{j=1}^{J_t} \rho_t^j \cdot [C_{gf,t} \cdot P_{gf,t}^j - C_{gt,t} \cdot P_{gt,t}^j + C_{gas,t} \cdot (F_{chp,t}^j + F_{boi,t}^j)] \end{aligned}$$

Electric balance

$$P_{gf,t}^j - P_{gt,t}^j + P_{chp,t}^j + P_{bd,t}^j - P_{bc,t}^j + P_{sol,t}^j = P_{nc,t}^j + P_{cntr,t} \cdot x_{ele,t}^j$$

$$0 \leq P_{gf,t}^j \leq M_{gf} \cdot x_{gf,t}^j$$

$$0 \leq P_{gt,t}^j \leq M_{gt} \cdot x_{gt,t}^j$$

$$x_{gf,t}^j + x_{gt,t}^j \leq 1$$

$$S_{bat,t+1}^j = S_{bat,t}^j + (\eta_{bc} \cdot P_{bc,t+1}^j - P_{bd,t+1}^j / \eta_{bd}) \cdot T_d / C_{bat}^{\max}$$

$$P_{bc}^{\min} \cdot x_{bc,t}^j \leq P_{bc,t}^j \leq P_{bc}^{\max} \cdot x_{bc,t}^j$$

$$P_{bd}^{\min} \cdot x_{bd,t}^j \leq P_{bd,t}^j \leq P_{bd}^{\max} \cdot x_{bd,t}^j$$

$$x_{bc,t}^j + x_{bd,t}^j \leq 1$$

Thermal balance

$$\eta_{hc} (H_{chp,t}^j + H_{boi,t}^j) = H_{nc,t}^j + H_{cntr,t} \cdot x_{heat,t}^j$$

$$F_{chp,t}^j = \alpha \cdot P_{chp,t}^j + \beta \cdot x_{chp,t}^j$$

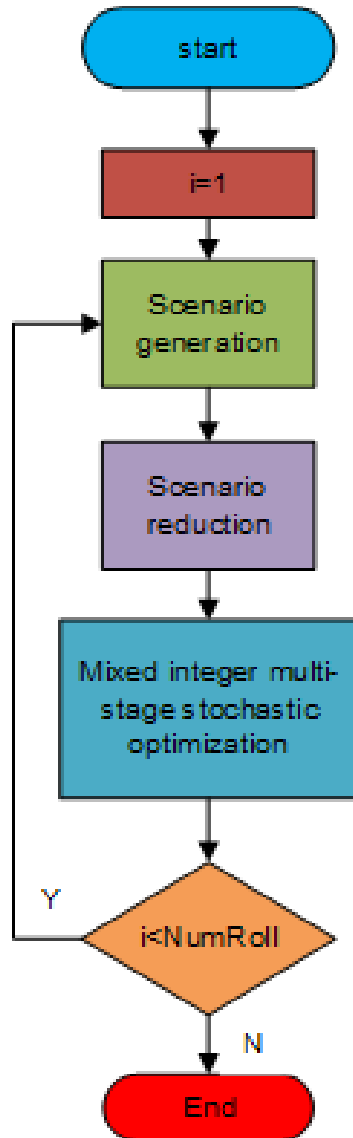
$$H_{chp,t}^j = \eta_{hre} (F_{chp,t}^j - P_{chp,t}^j)$$

$$P_{chp}^{\min} \cdot x_{chp,t}^j \leq P_{chp,t}^j \leq P_{chp}^{\max} \cdot x_{chp,t}^j$$

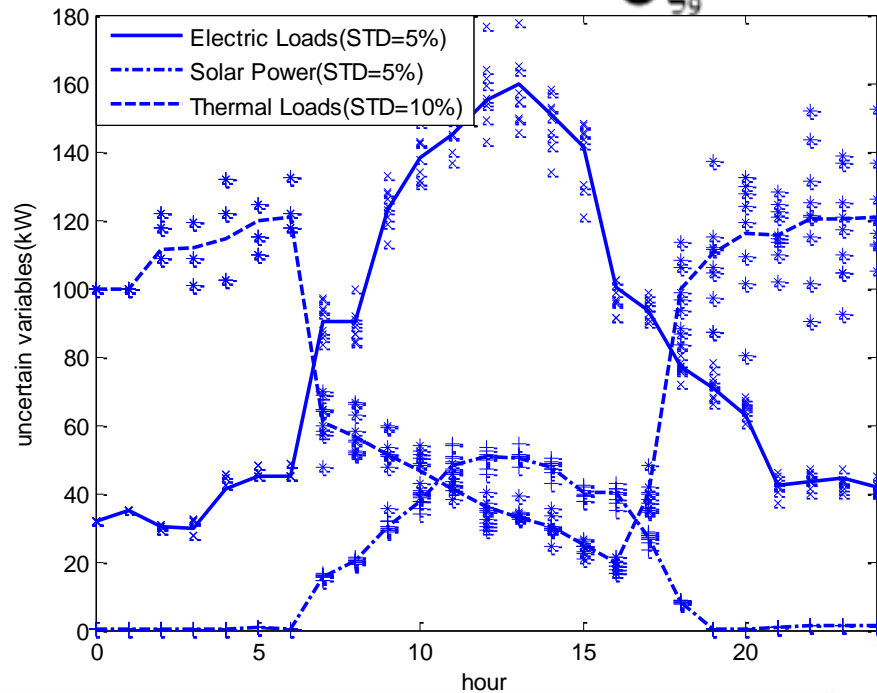
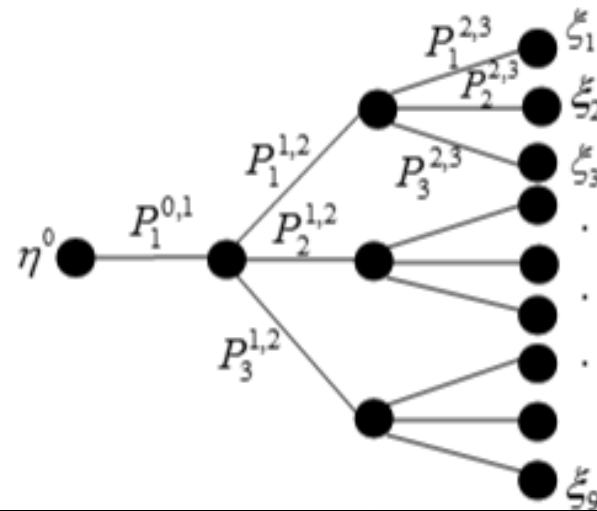
$$H_{boi,t}^j = \eta_{boi} \cdot F_{boi,t}^j$$

$$H_{boi}^{\min} \cdot x_{boi,t}^j \leq H_{boi,t}^j \leq H_{boi}^{\max} \cdot x_{boi,t}^j$$

# Solution Methodology

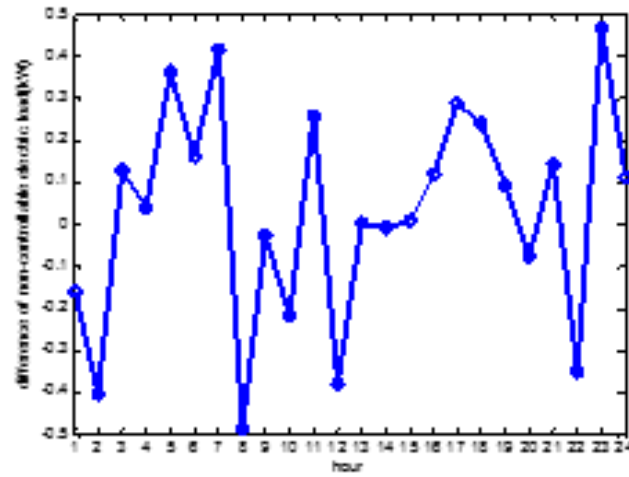
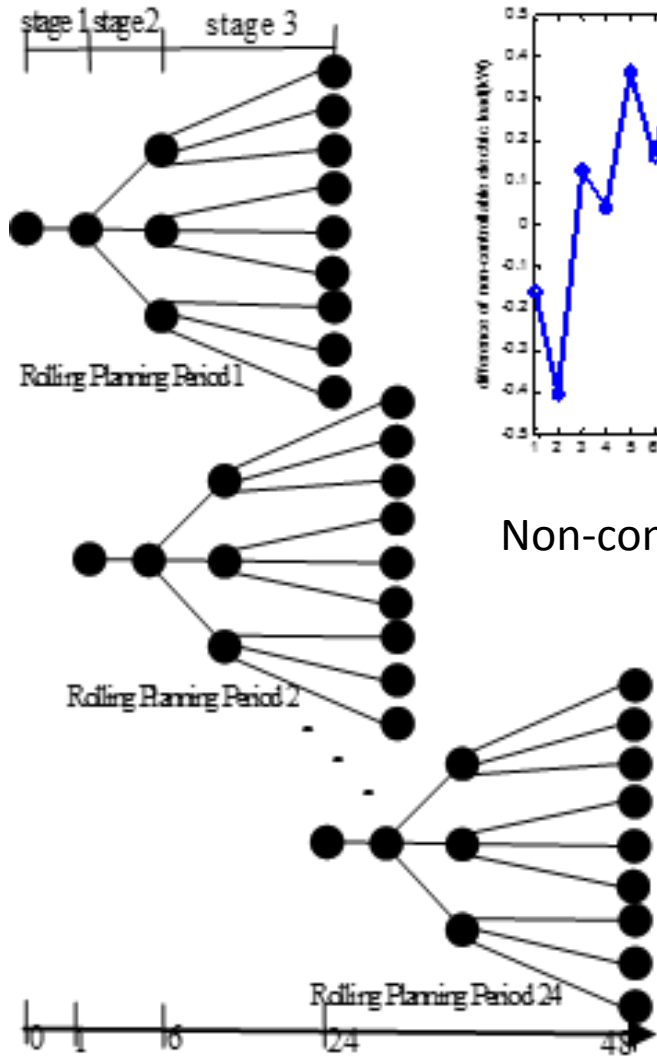


Flow chart

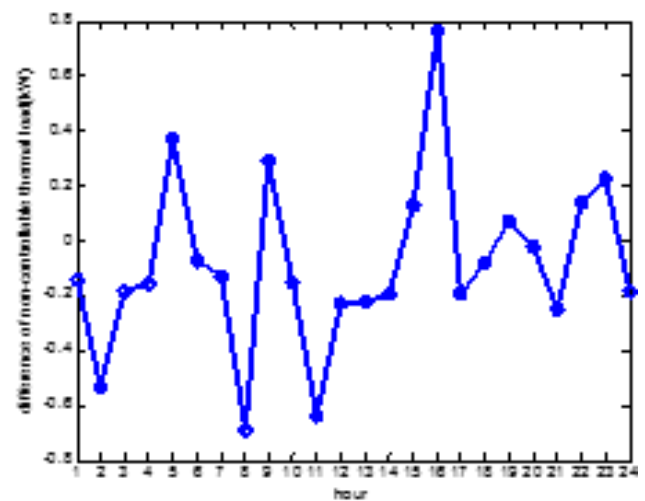




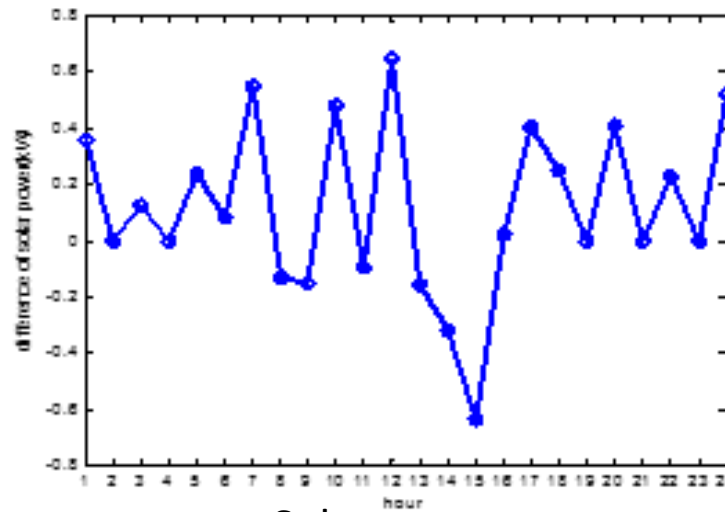
# Solution Methodology



Non-controllable electric load



Non-controllable thermal load



Solar power

Rolling difference for uncertainties

# Case Studies

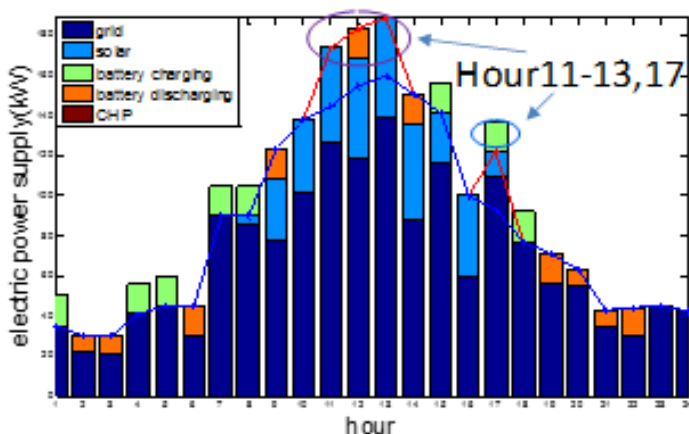
Cases		1	2	3	4	5	6(Stochastic)
Power Generation	Electric Grid	✓	✓	✓	✓	✓	✓
	Solar	×	✓	✓	✓	✓	✓
	Battery	×	×	✓	✓	✓	✓
	CHP	×	×	×	×	✓	✓
	Boiler	×	×	×	✓	✓	✓
Household Loads	NC electric loads	✓	✓	✓	✓	✓	✓
	Controllable Electric Loads	-	-	-	...	...	...
	NC Heat Loads	×	×	×	✓	✓	✓
	Controllable Heat Loads	×	×	×	...	...	...

‘NC’ means non-controllable; ‘✓’ means candidate; ‘×’ mean non-candidate; ‘-’ means fixed status; ‘...’ means unfixed status

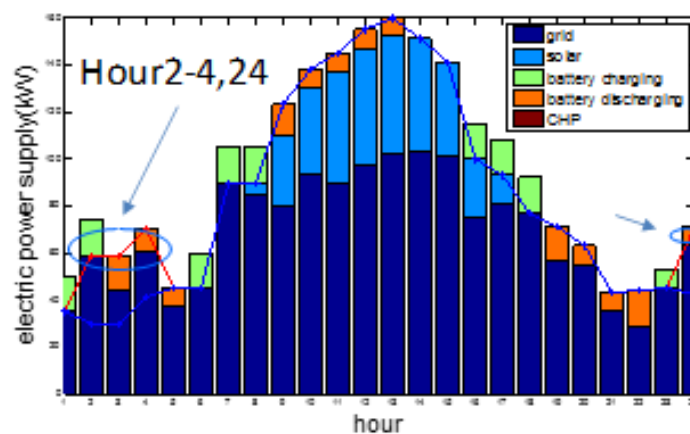
## Daily production cost (\$)

Case	1	2	3	4	5	6
Cost	196.80	155.67	150.32	221.08	195.49	216.54

# Electric Power Supply

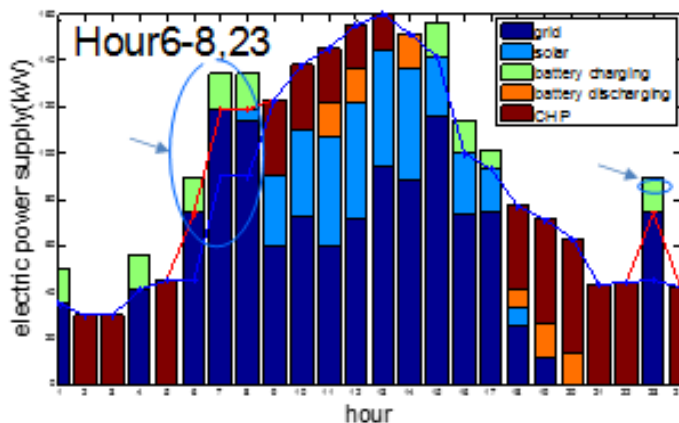


Case 3

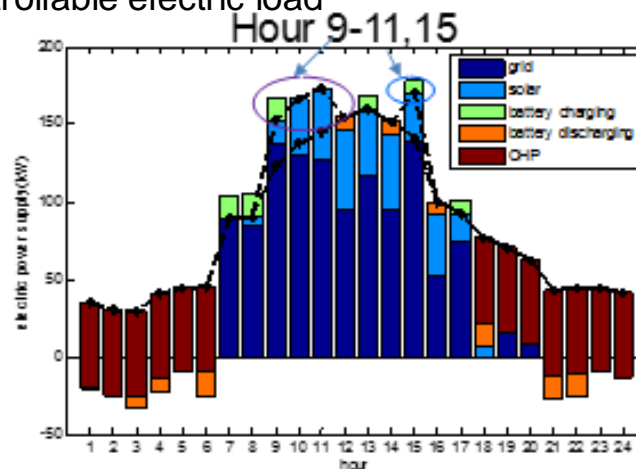


Case 4

Fixed V.S unfixed controllable electric load

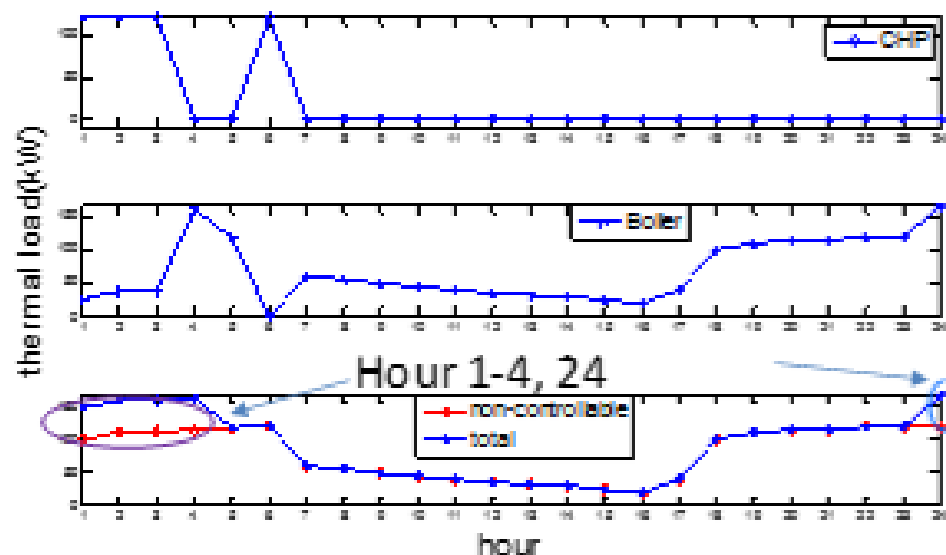
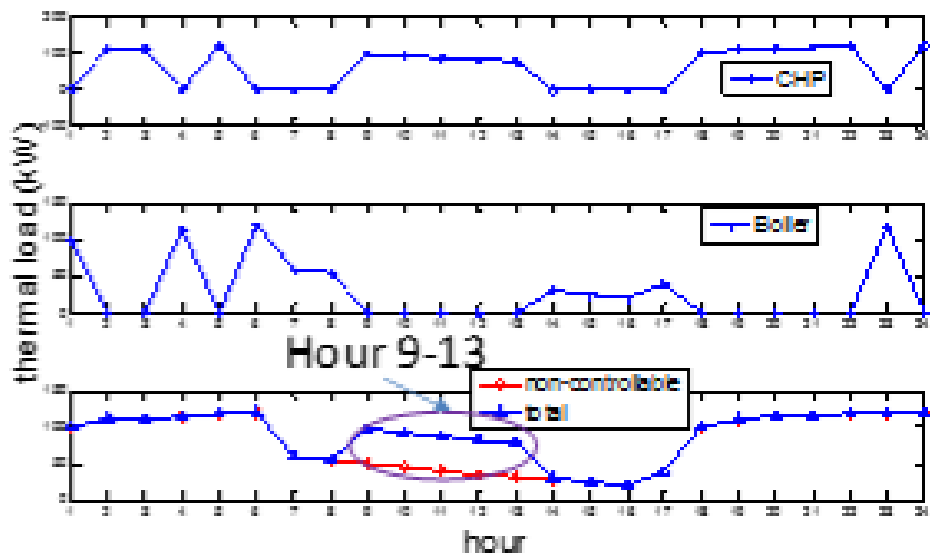


Case 5: deterministic



Case 6: stochastic

# Thermal Power Supply



# Conclusions

- The optimization of energy distribution of buildings for time horizons of one day is considered as a multistage stochastic optimization problem.
- The incorporation of uncertainties about solar power production, non-controllable electric and heat loads in the optimization model is considered through a multistage scenario tree.
- A manageable number of scenarios are considered by the backward scenario reduction method.
- Rolling scheduling will take into account the updated information on a continuous hourly basis for uncertainties, including solar power production, non-controllable electric and heat loads .
- The consideration of uncertainties will introduce more cost for the operation of energy-efficiency building with CHP system.

**Q&A**  
**Thanks**